# MATHEMATICS PAPER IA.- MARCH 2011. ALGEBRA, VECTOR ALGEBRA AND TRIGONOMETRY.

## TIME : 3hrs

Note: This question paper consists of three sections A,B and C.

## SECTION A

**VERY SHORT ANSWER TYPE QUESTIONS.** 

Note : Attempt all questions. Each question carries 2 marks.

1. If 
$$A = \left\{0, \frac{\pi}{6}, \frac{\pi}{3}, \frac{\pi}{4}, \frac{\pi}{2}\right\}$$
 and f:A  $\rightarrow$  B is surjection defined by f(x)=cosx

then find B

- 2. If  $f(x)=5^x$  then find  $f^{-1}(x)$
- 3. If the position vectors of points A,B are -2i+j-k,-4i+2j+2k,and 6i-3j-13k respectively and AB= $\lambda$  AC find  $\lambda$
- 4. Find the vector equation line joining points 2i+j+3k and -4i+3j-k

5. If  $4i+2\frac{p}{3}j+pk$  is parallel to the vector i+2j+3k find p

6. Prove that  $\cos 340 \cos 40 + \sin 200 \sin 140 = 1/2$ 

7. Show that 
$$\frac{\cos 9 + \sin 9}{\cos 9 - \sin 9} = \cot 36$$

8. If coshx = 5/2 find the value of i) cosh(2x) ii) sinh2x

- 9. If a=26 cm b=30 cm  $\cos C=63/65$  then find c
- 10. Write  $Z = -\sqrt{7} + i\sqrt{21}$  in polar form

#### **SECTION B**

#### SHORT ANSWER TYPE QUESTIONS.

5X4 =20

Note : Answer any FIVE questions. Each question carries 4 marks.

11 .If a,b,c are non coplanar vectors then prove that the vectors 5a+6b+7c,7a-8b+9c and 3a+20b+5c are coplanar 12 Find the volume of the percellelepined with extermineus

- 12. Find the volume of the parallelepiped with coterminous edges 2i-3j,i+j-k,3i-k
- 13. Prove that  $\left(1+\cos\frac{\pi}{8}\right)\left(1+\cos\frac{3\pi}{8}\right)\left(1+\cos\frac{5\pi}{8}\right)\left(1+\cos\frac{7\pi}{8}\right)=\frac{1}{8}$
- 14. solve  $1+\sin^2\theta=3\sin\theta\cos\theta$
- 15. Prove that  $\tan^{-1}(\frac{1}{2}) + \tan^{-1}\frac{1}{5} + \tan^{-1}\frac{1}{8} = \frac{\pi}{4}$

Max. Marks.75

10X2 = 20

16. If a,b,c are in A.P. then show that  $\tan \frac{A}{2} \cos \frac{C}{2} = 1$ 17. Show that  $16 \sin^5 \theta = \sin 5 \theta - 5 \sin 3 \theta + 10 \sin \theta$ 

# SECTION C

LONG ANSWER TYPE QUESTIONS.5X7 =35Note: Answer any Five of the following. Each question carries 7 marks.18 .Let f:  $A \rightarrow B$  and g:  $B \rightarrow C$  be bijection. Then  $(gof)^{-1} = f^{-1}og^{-1}$ 19 .Prove By Mathematical Induction Show that $a + ar + ar^2 \dots = \frac{a(r^n - 1)}{r - 1}$ 20 Find the equation Plane passing from points A(2, 3, -1) B(4, 5, 2) and

20 .Find the equation Plane passing from points A(2,3,-1),B(4,5,2) and C(3,6,5)

21. Prove that 
$$\sin\frac{A}{2} + \sin\frac{B}{2} + \sin\frac{C}{2} = 1 + 4\sin\left(\frac{\pi - A}{4}\right)\sin\left(\frac{\pi - B}{4}\right)\sin\left(\frac{\pi - C}{4}\right)$$
  
22. If  $a = (b - c)\sec\theta$  prove that  $\tan\theta = \frac{2\sqrt{bc}}{b-c}\sin\frac{A}{2}$ .

23. From the top of a tree on the bank of a lake, an Aeroplane in the sky makes an angle of elevation  $\alpha$  and its image in the river makes an angle of depression  $\beta$ . if the height of the tree from the water surface is 'a' and that of the height of the aero plane is h, show that  $h = \frac{a \sin(\alpha + \beta)}{\sin(\beta - \alpha)}.$ 

If  $\alpha, \beta$  are roots of the equation  $x^2 - 2x + 4 = 0$  then for any value n show that 24.  $\alpha^n + \beta^n - 2^{n+1} \cos(\frac{n\pi}{2})$ 

$$\alpha^n + \beta^n = 2^{n+1} \cos(\frac{1}{3})$$